

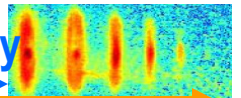


MAX BORN -
INSTITUTE

Attosecond multielectron dynamics
in tunnel ionization

Olga Smirnova
Max-Born Institute

MBI-Theory



Theory

Experiment



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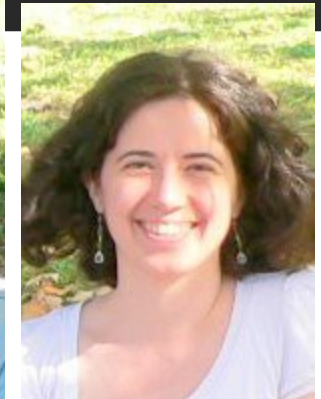
**Yann Mairesse ,
CELIA, Bordeaux**



**Nirit Dudovich ,
Weizmann Institute,**



**Dror Shafir ,
Weizmann
Institute,**

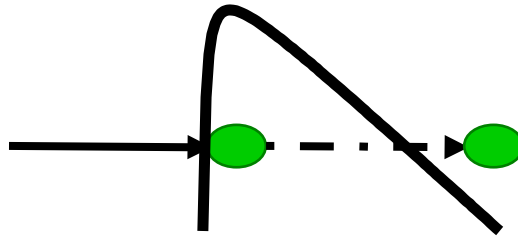


**Hadas Soifer,
Weizmann
Institute,**

+ Misha Ivanov, MBI & Imperial College

MBI-Theory

Time-resolving tunneling dynamics



Time delays in tunneling: old and controversial

(recent experiments: U. Keller group, Science, 322, 1525, 2008)

Tunneling dynamics can be affected/probed via coupling to other degrees of freedom
- how do they respond?

Examples:

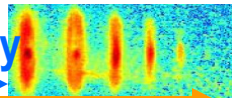
Josephson junction:

energy loss during tunneling due to friction

Metal-insulator tunneling:

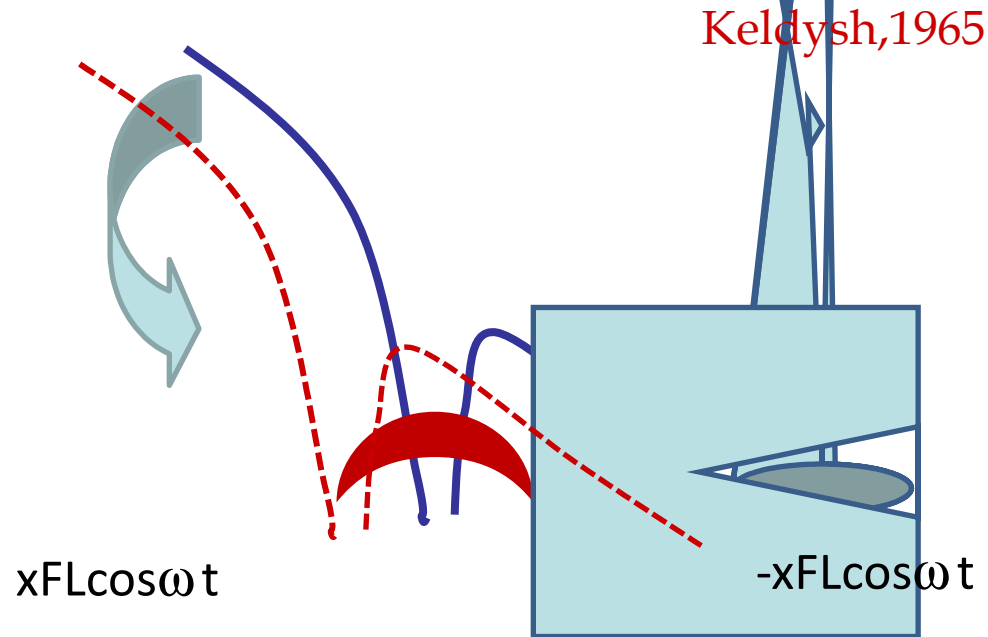
build-up of image charge

Strong-field ionization of molecules: electron-hole interaction in tunneling



Strong-field ionization in IR fields

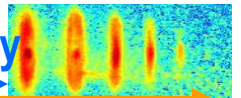
$\omega/I_p \ll 1$ – adiabatic tunnelling perspective on ionization.



$$aT \sim \exp[-(2I_p)^{3/2}/3FL]$$

Optical tunneling in the oscillating laser field is the main ionization mechanism for $\omega \ll I_p$

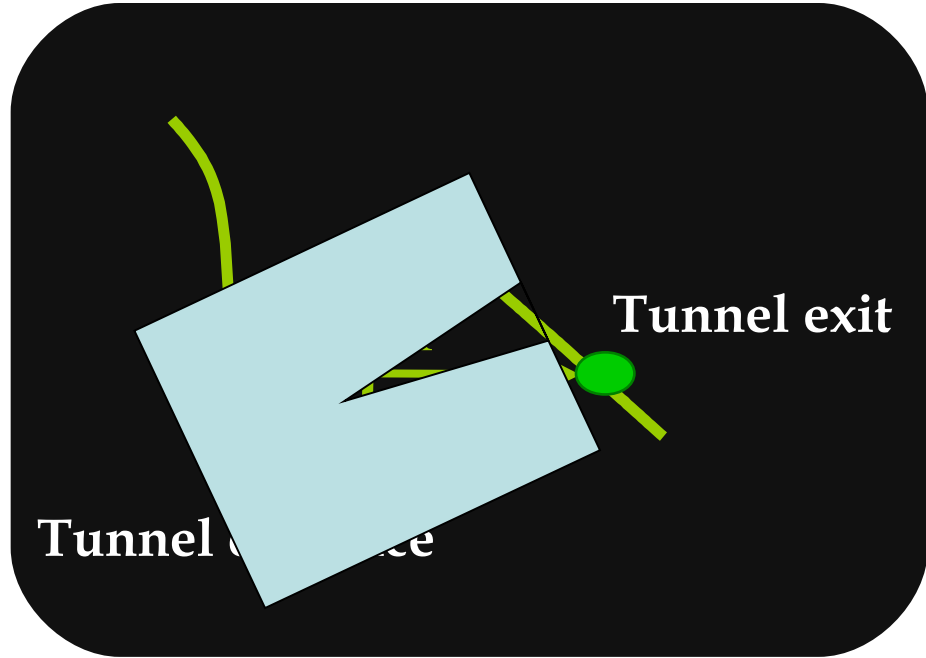
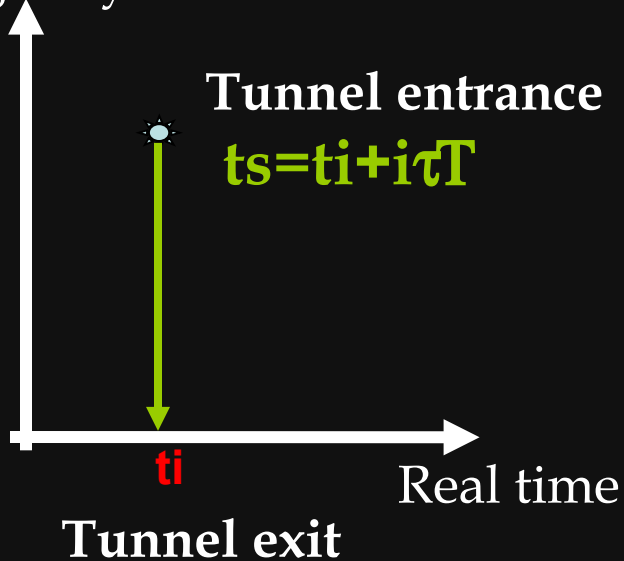
M B I - Theory



Semiclassical perspective on tunneling

Electron trajectory during tunneling: imaginary velocity & imaginary time

Imaginary time



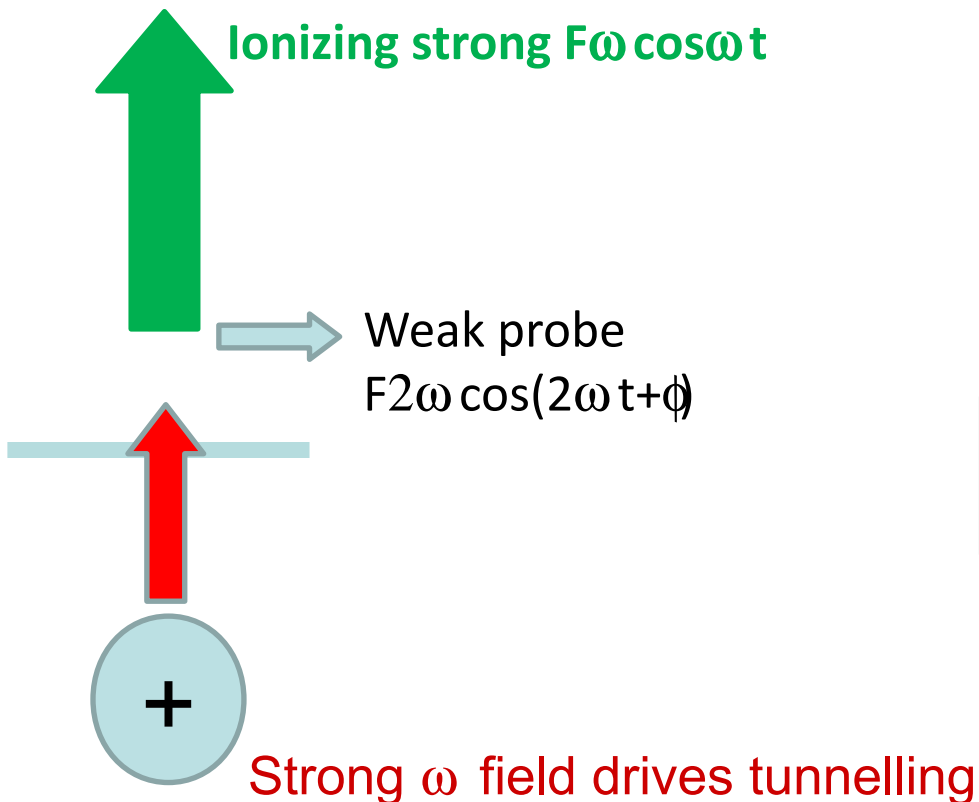
t_s - time of entering the barrier, t_i - time of exiting the barrier;

τT - time spent under barrier: imaginary

Does this theory fit experiment? Need to:

- Tag each electron trajectory as it exits the barrier at t_i
- Check if distribution of t_i fits the theory picture above

Tagging trajectories as they are launched



Strong ω field drives tunnelling

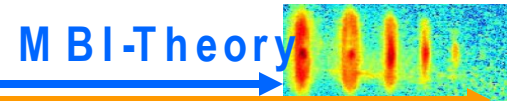
Weak 2ω tags the electron

Dependence of Δv and Δr on ϕ encodes ionization times

$$v(t, t_i) = \int_{t_i}^{t_r} F_2(t') A_2(t_r) A_2(t_i) dt'$$

$$r(t, t_i) = \int_{t_i}^{t_r} v(t', t_i) dt'$$

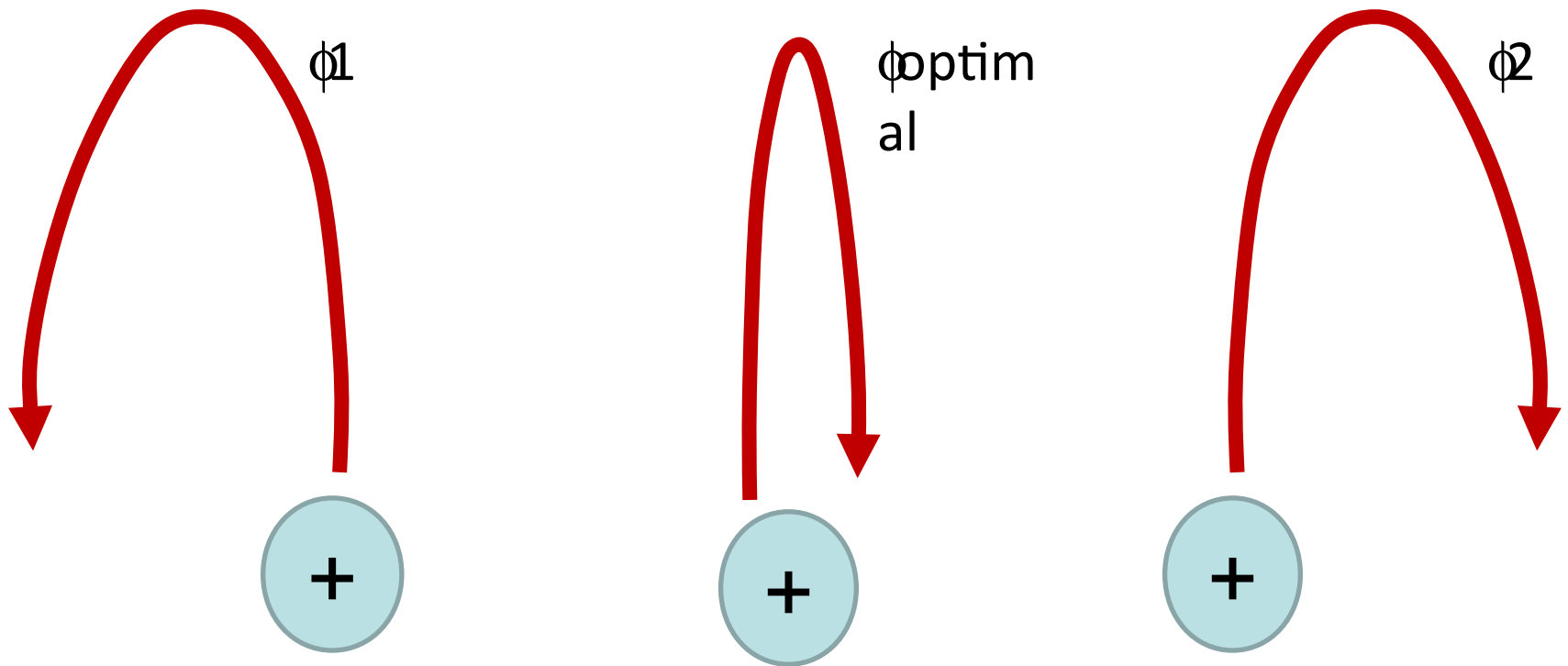
Δv and Δr are recorded in harmonic spectra



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Measuring position shifts: High harmonic signal

Oscillating field brings the electron back – harmonic emission
Parent ion is a perfect measurement device

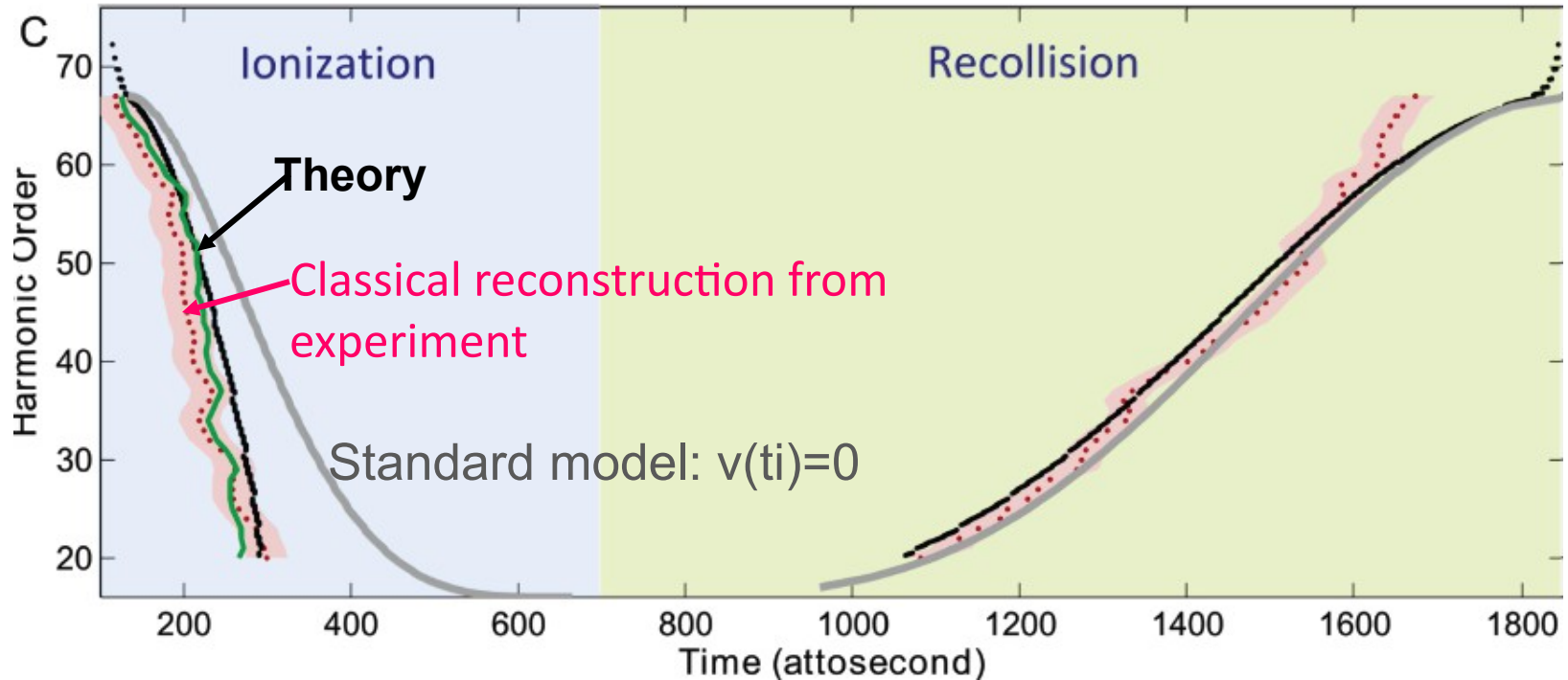


Odd harmonic intensities maximize for minimal $\Delta r(\phi)$
Odd harmonics measure $\Delta r(\phi)$

Reconstructed times in Helium

Helium, 40 fsec pulse, 800 nm at 4×10^{14} W/cm², 400 nm at 1-2% intensity level

D. Shafir et al, Nature 2012

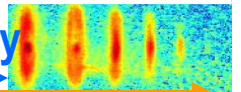


Green: Full quantum, including effect of 2ω on ionization

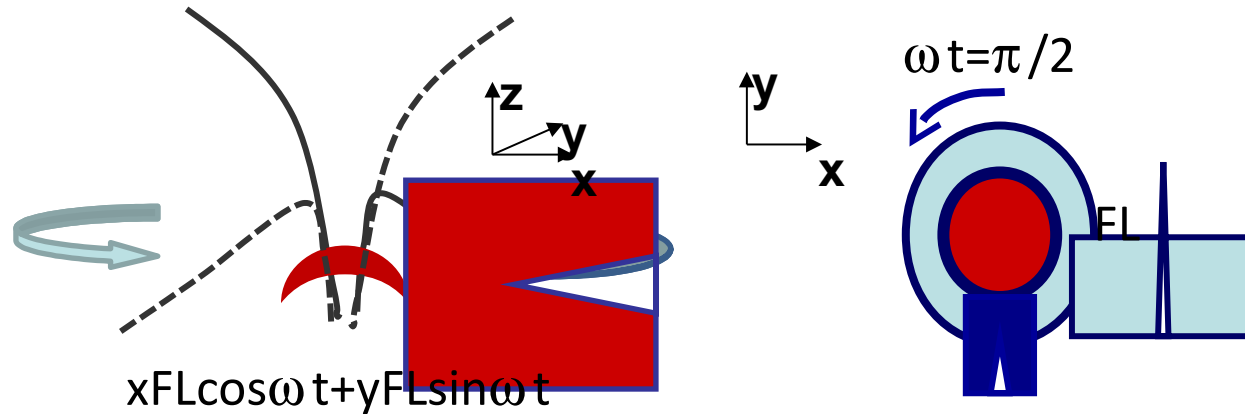
Results are consistent with the theory: purely imaginary 'delay'

Are there any kinematic consequences of "dynamics in imaginary time"?

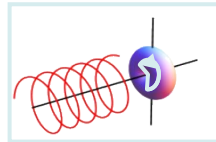
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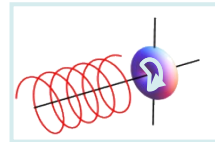
Tunneling in circularly-polarized IR fields



p+ orbital



p- orbital



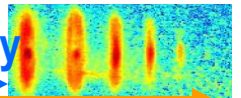
No real delays: laser field does not rotate during tunneling

Co-rotating and counter-rotating electron would tunnel with the same rate

Real delays: laser field rotates during tunneling

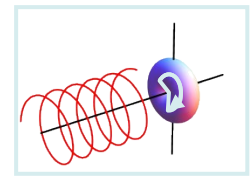
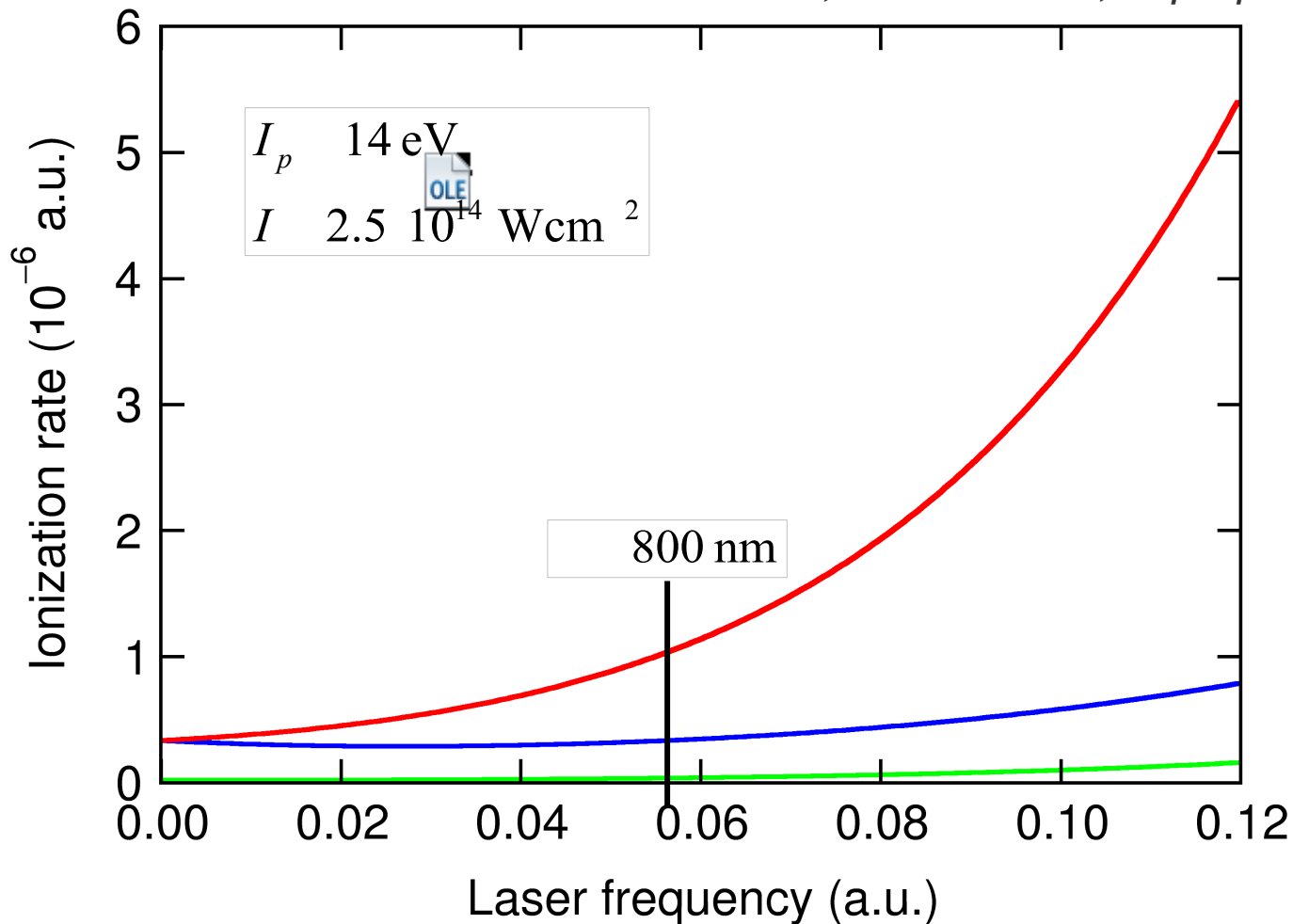
Co-rotating electron tunnels easier

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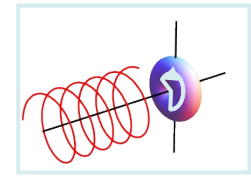


Result for Kr: Counter-rotating electron tunnels easier!

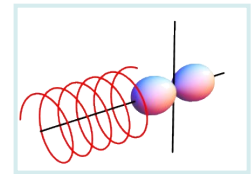
- I. Barth, O. Smirnova, *Phys. Rev. A* **84**, 063415 (2011)
- J. Kaushal, O. Smirnova, *in preparation*



p-orbital

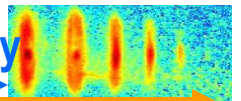


p+ orbital



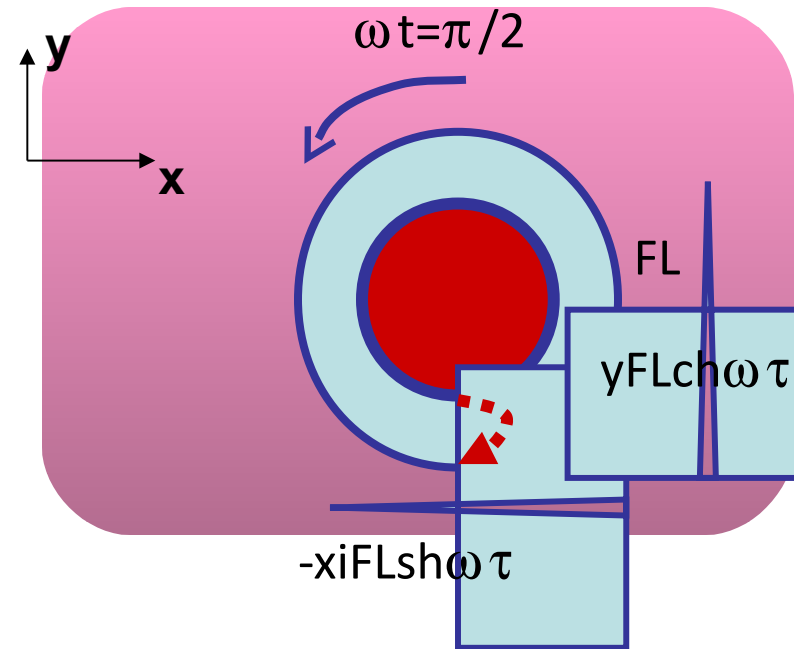
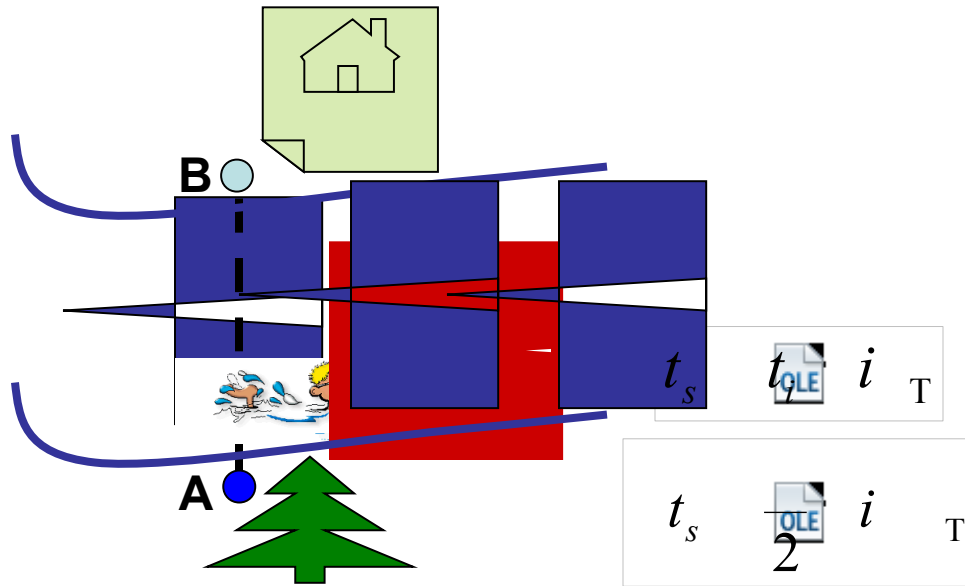
p0 orbital

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Why does the counter-rotating electron tunnel easier?

Initial electron velocity prior to ionization is opposite to the rotation of the field



$$\text{Laser field} = -x_i F L \text{sh} \omega \tau + y F L \text{ch} \omega \tau$$

Ion is created in polarized state- probe by transient absorption
Tunneling dynamics is recorded in the response of the ion

Hole dynamics in space and time

Time:

- When is the hole created?
- Is there a delay in hole formation?
- Does the hole move or remains static?

Space:

- Is the hole aligned along the direction of electron emission?

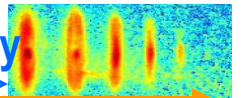
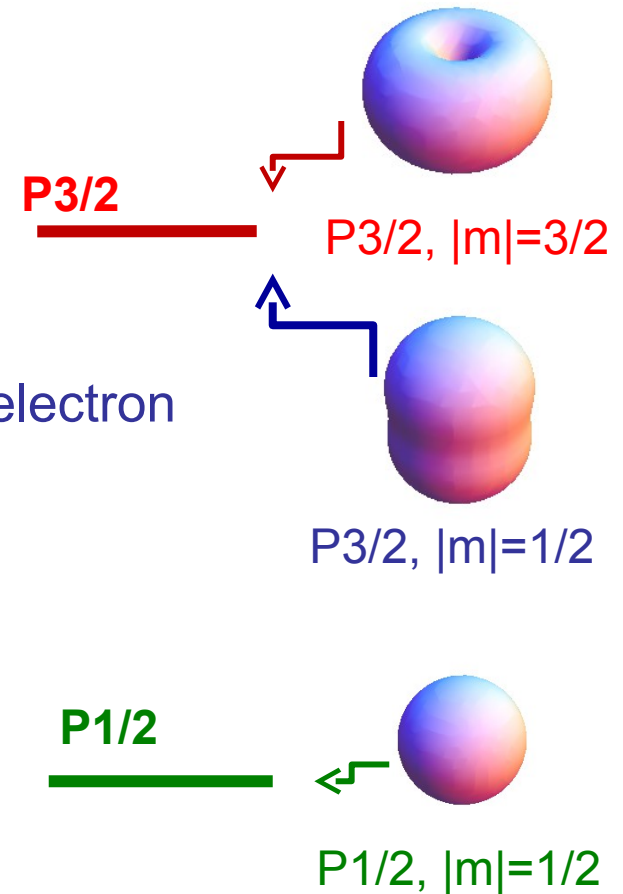
Initial kick:

- Is there “electron-hole” recoil?

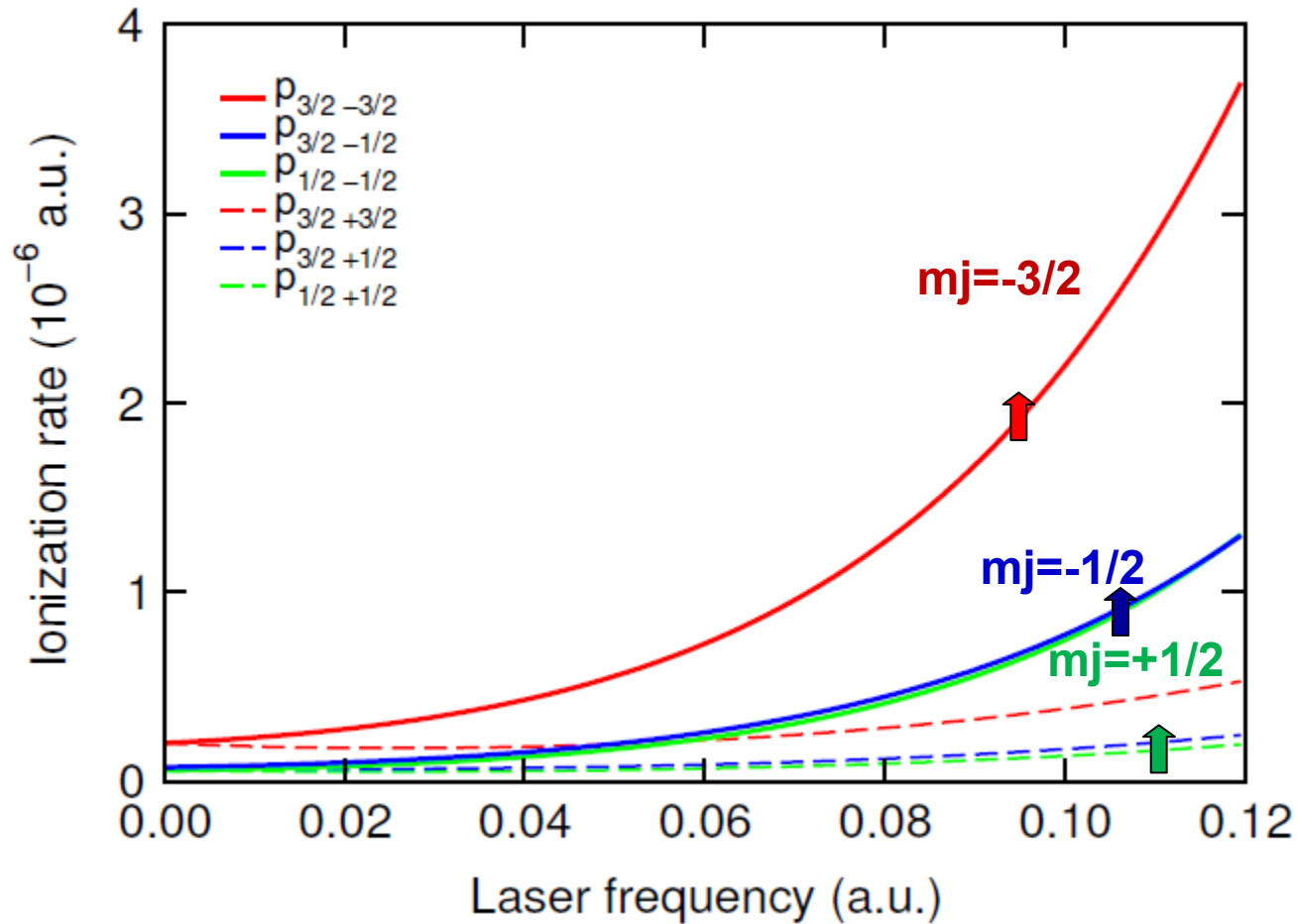
Need to find:

- Initial populations of hole states
- Relative phases between them
- Must take spin into account

Hole states in Kr



Populations of hole states in Kr



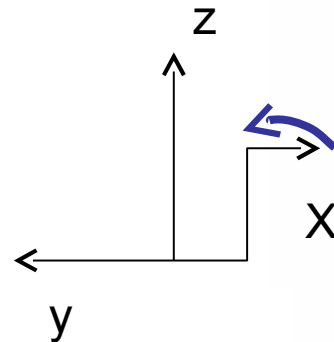
More spin-down states than spin-up, for right circular field:
consequence of higher ionization rate for $m=-1$

Hole dynamics in Kr: 800nm 2.5 10¹⁴ W/cm²

~Up electron- Rotating hole



2Up+1p electron- Swinging hole



↑ Spin up

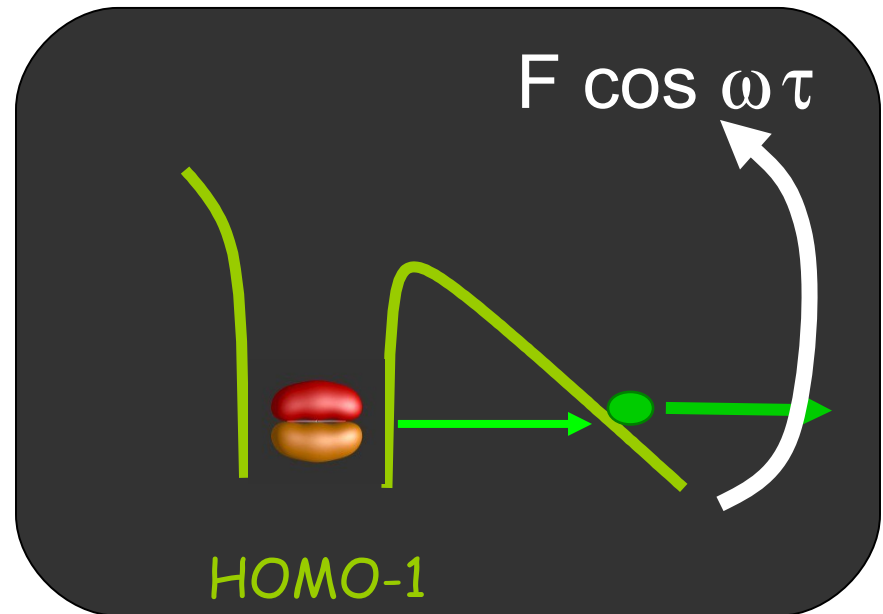
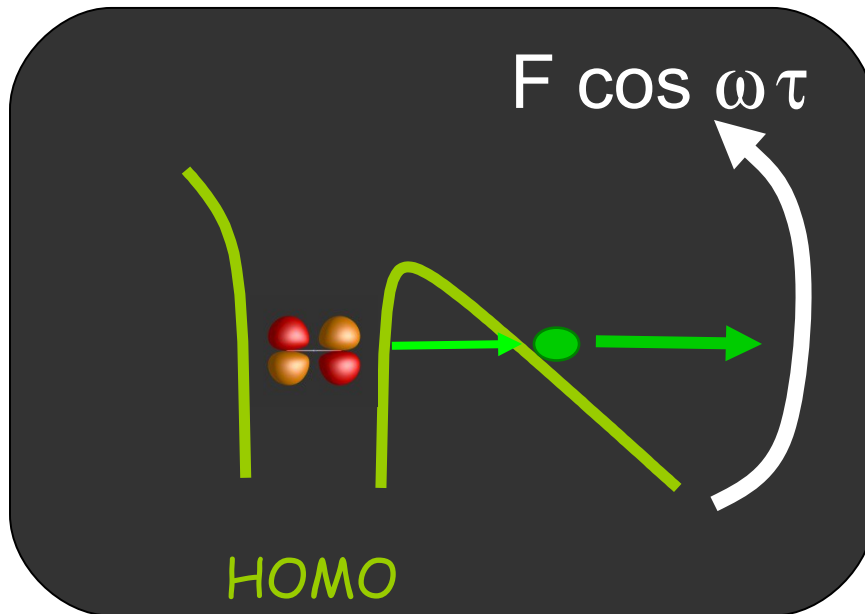
↓ Spin down

Theory shows:

- Electron-hole entanglement plays crucial role
- Hole is aligned along the instantaneous direction of electron emission
- No delays (in multielectron case with no channel interaction)

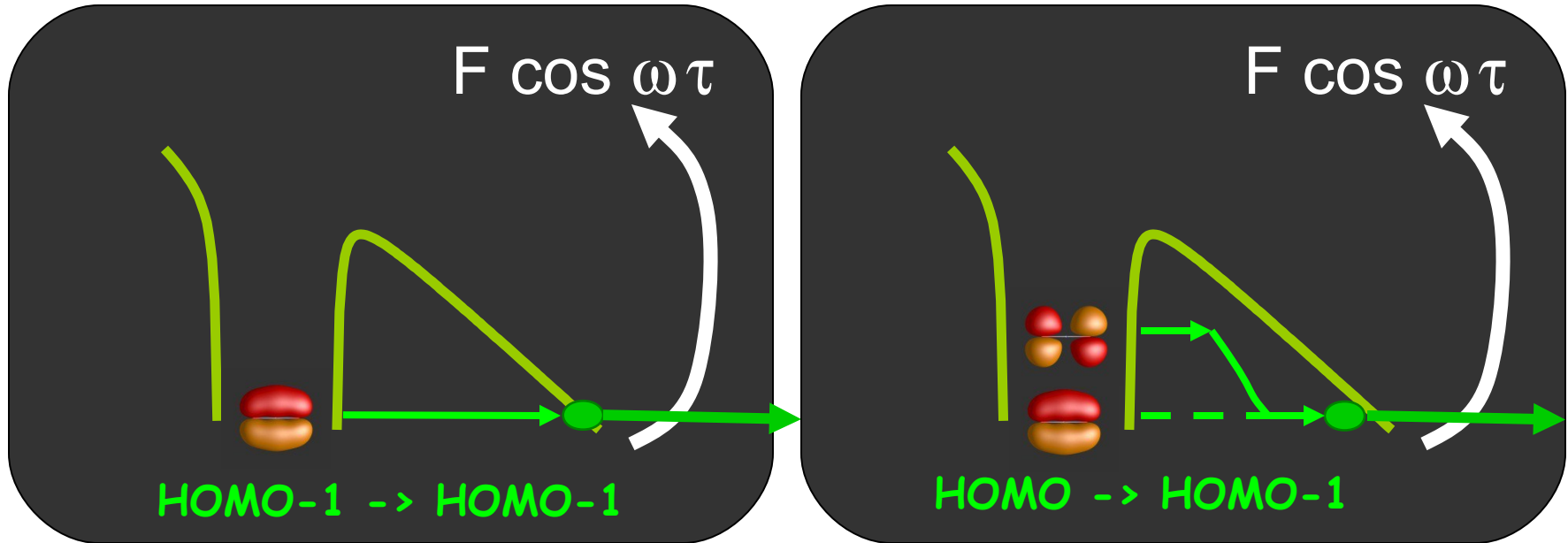
Tunneling for coupled channels

Tunneling from lower orbitals: usually expect exponential suppression for deeper orbitals



This talk: Role of electron correlation during tunneling - overcoming exponential suppression

Idea: new tunneling channels



Direct channels

Cross channel

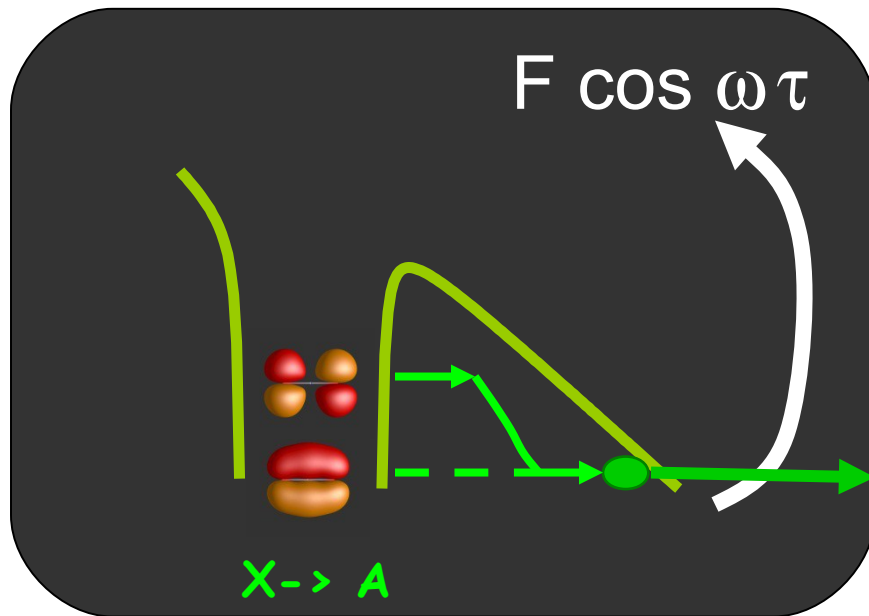
- Tunneling electron excites the core while moving through the barrier
- This channel is not subject to the full exponential suppression characteristic of the direct tunnel ionization from deeper orbitals.

Z. Walters, O. Smirnova J. Phys B 2010

L. Torlina, M. Ivanov, Z. Walters, O. Smirnova PRA, in press

Coupled electron- ion dynamics: the ion

Ion: few-level system driven by the laser field and correlation “pulse”
(in complex time)



$$aX \rightarrow A(p) = cXA aX(p)$$

$$c_{mn} = \int_0^t dt V_{corr}^{mn}(t) e^{-I_p t}$$

t is the time left before exiting the tunnel.

Correlation -induced excitation is an integral of V_{corr} along the trajectory of the tunneling electron.

- Tunneling occurs in imaginary time
- Excitation amplitudes in the ion are the imprints of this dynamics

Comparison with numerical simulations



Serguei Patchkovskii, NRC, Ottawa

M. Spanner & S. Patchkovskii

Ab-initio close – coupling approach (**Phys Rev A, 2010**)

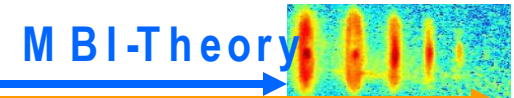
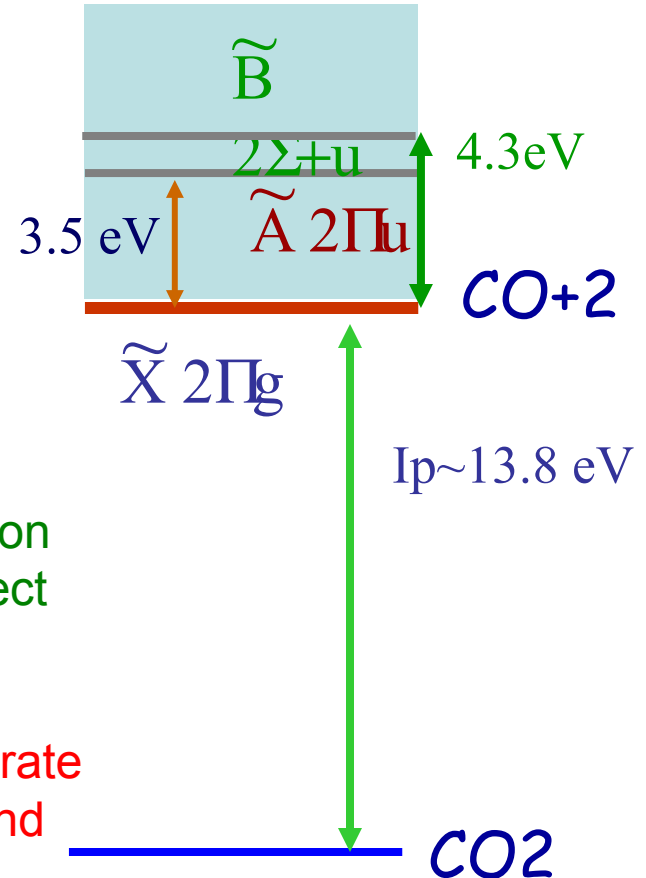
CO₂ I=1.3 10¹⁴ W/cm² ,
800 nm, half cycle pulse



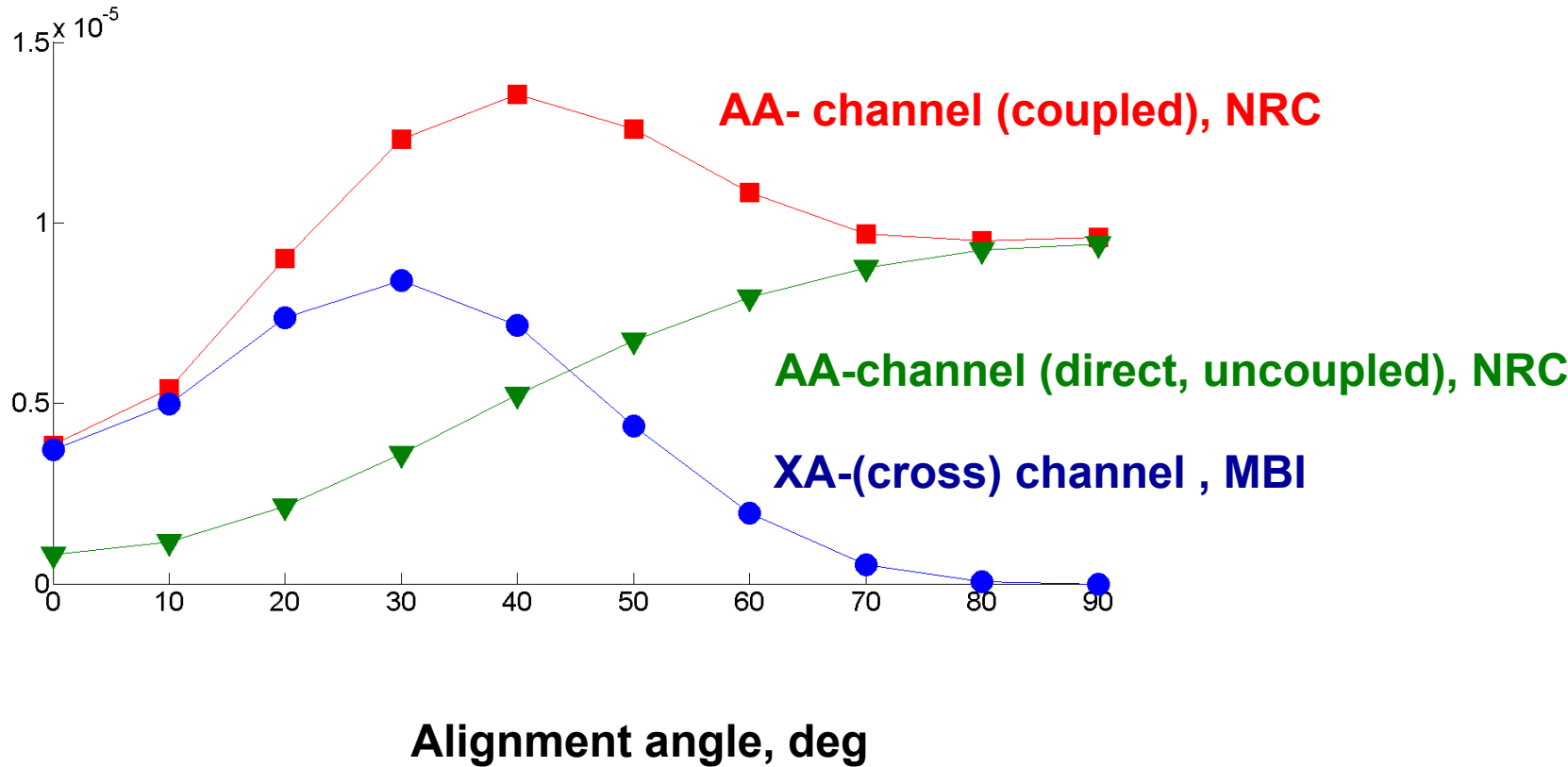
Michael Spanner, NRC, Ottawa

The NRC team made two simulations:

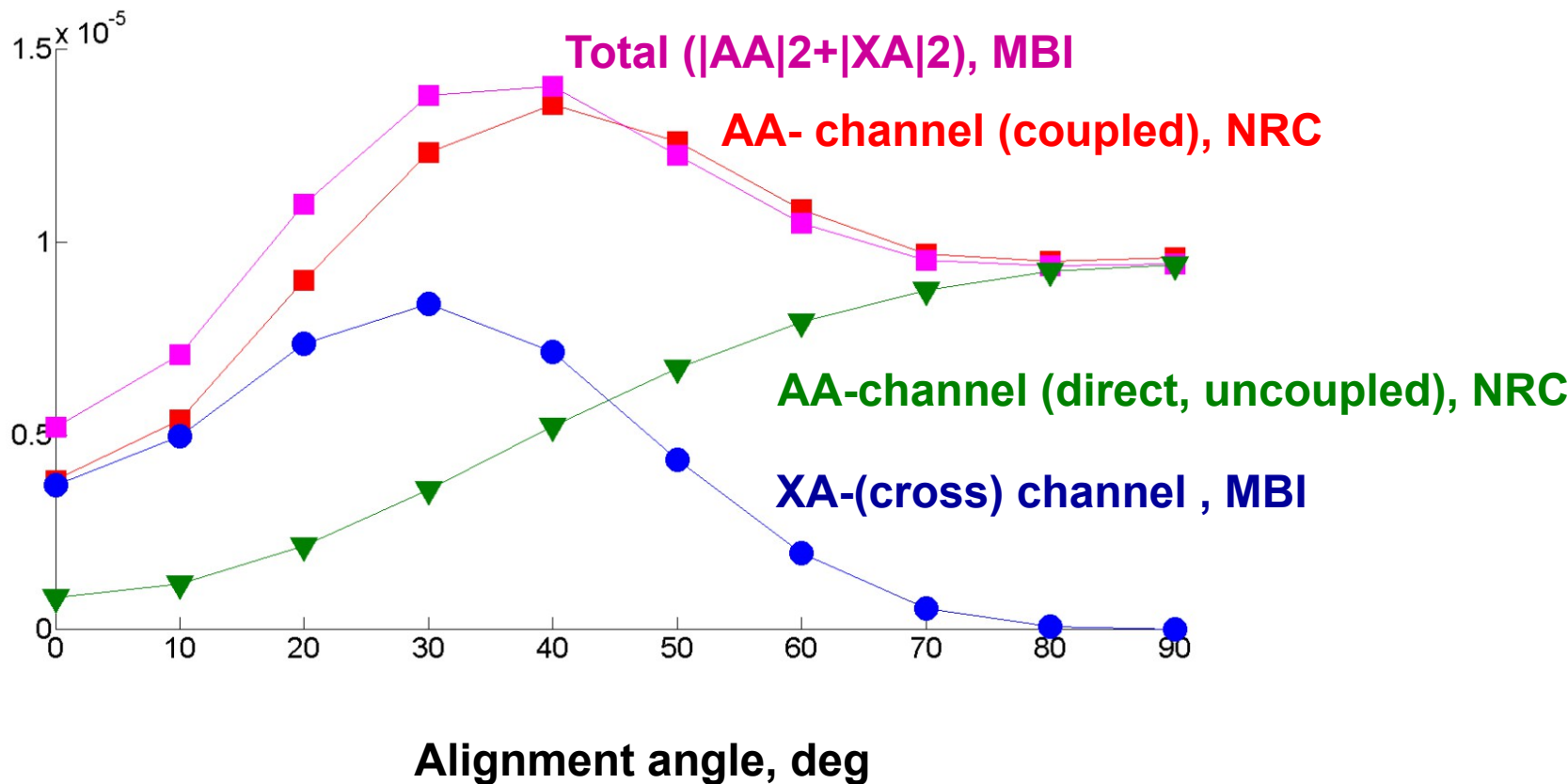
- Uncoupled channels: ionization rate in channel A includes direct channel only
- Coupled channels: ionization rate in channel A includes direct and cross-channels



Comparison numerical (NRC) vs analytical (MBI)

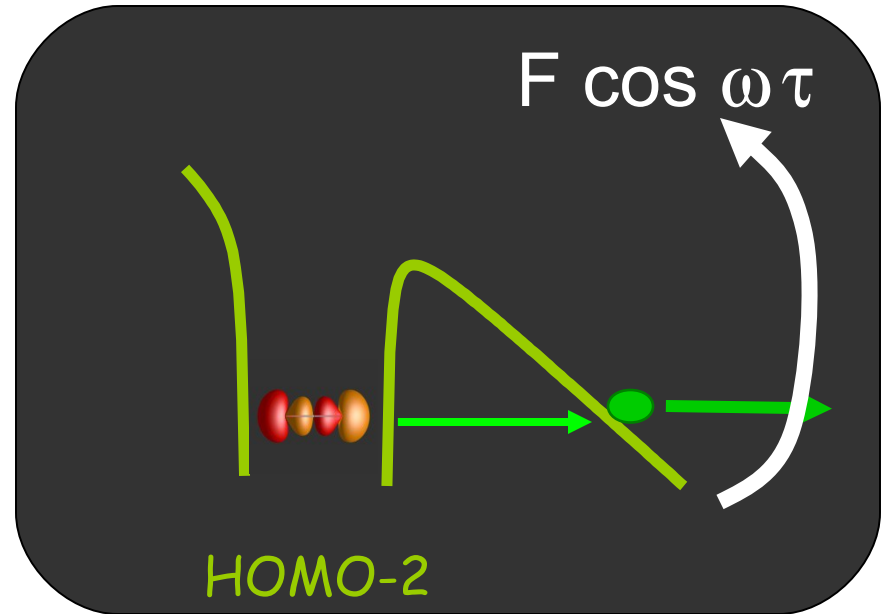
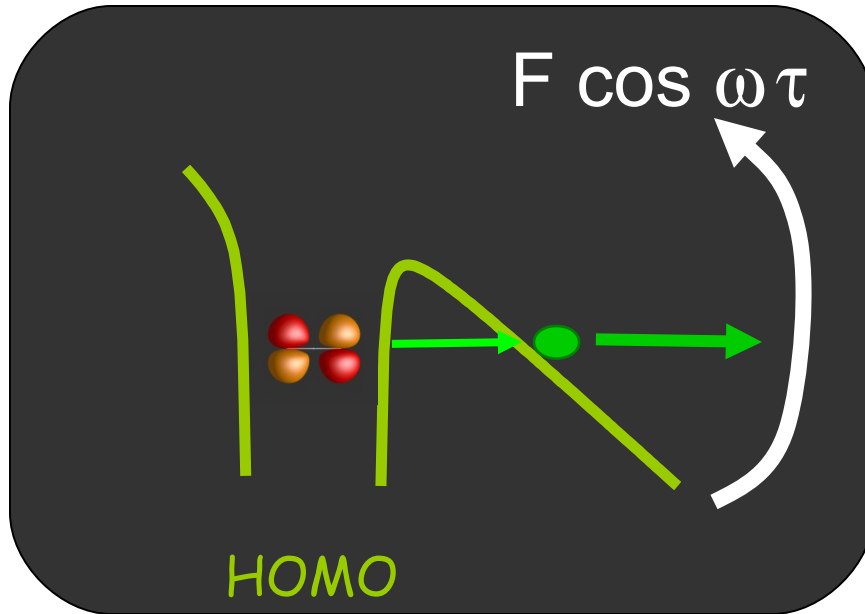


Comparison numerical (NRC) vs analytical (MBI)



Direct and cross channels should interfere: phase is close to $\pi/2$

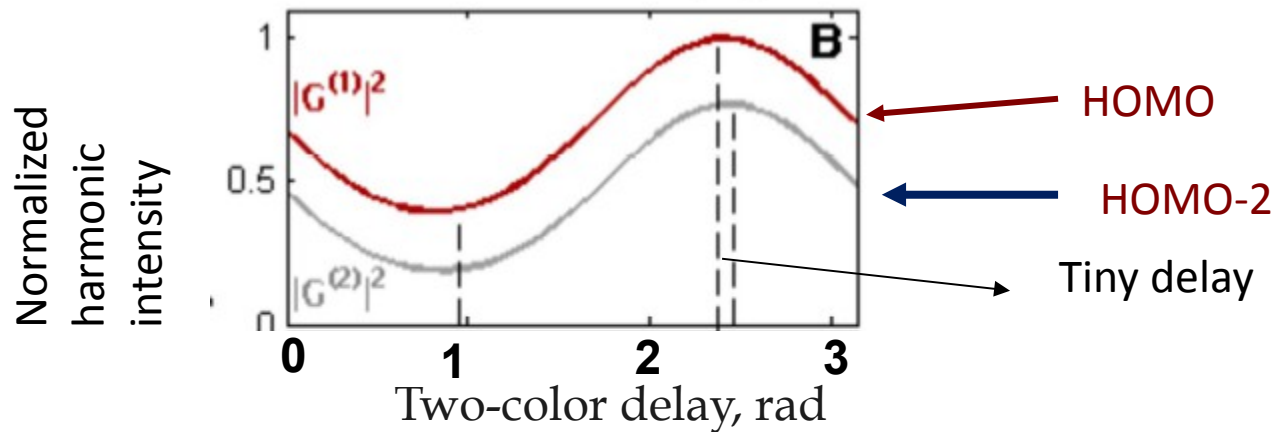
Time-resolving hole dynamic



Can we detect tunneling from two orbitals?

How to detect ionization from lower orbital?

Modulation of harmonic signal vs two-color delay



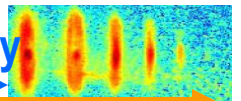
Strong $F\omega \cos\omega t$

Due to different ionization times, modulation for HOMO and HOMO-2 channels is slightly shifted

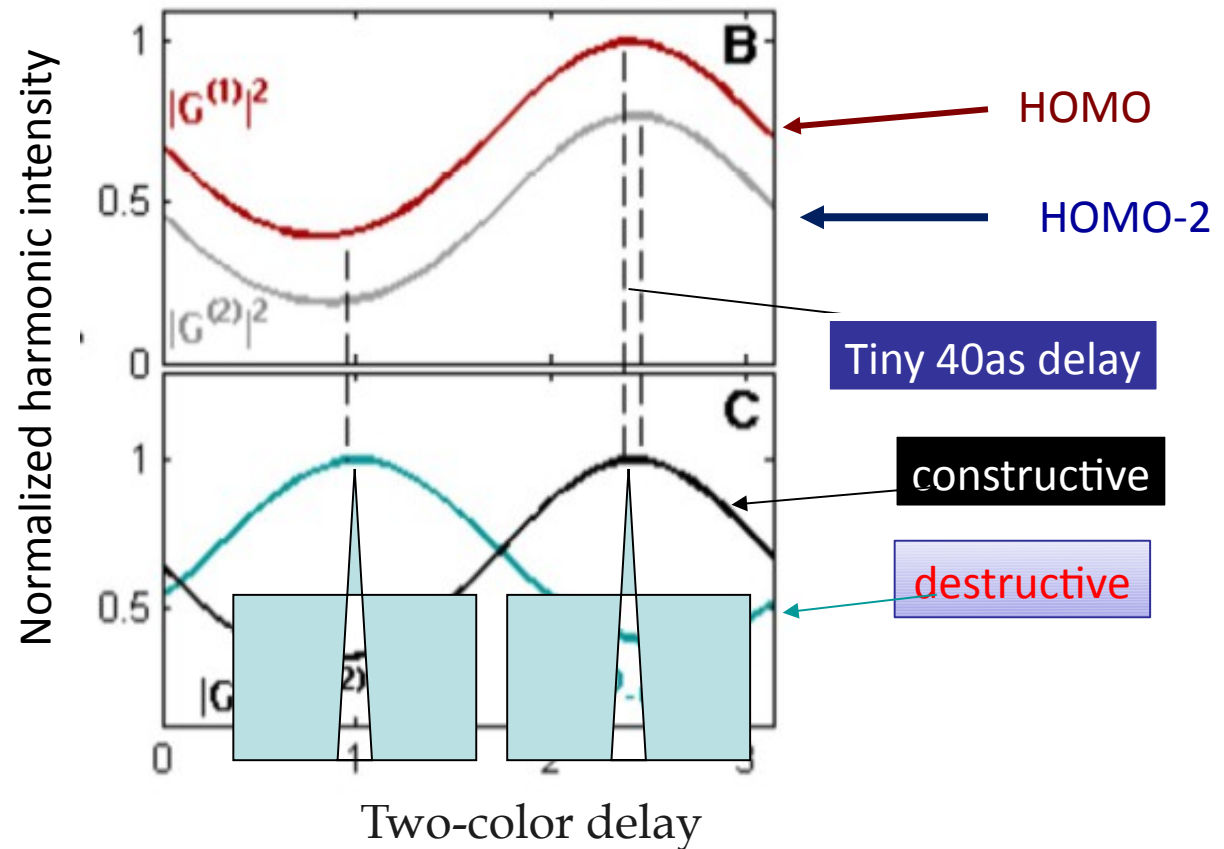
The shift is tiny. Can it be seen?

Weak probe
 $F2\omega \cos(2\omega t + \phi)$

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Detecting signal from two orbitals



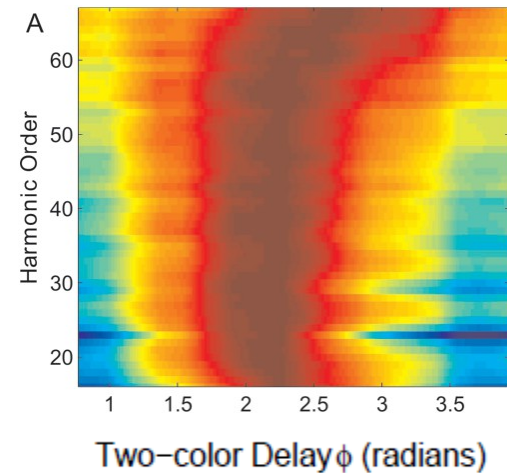
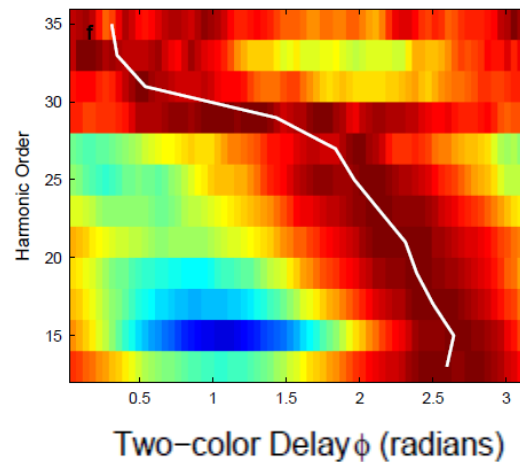
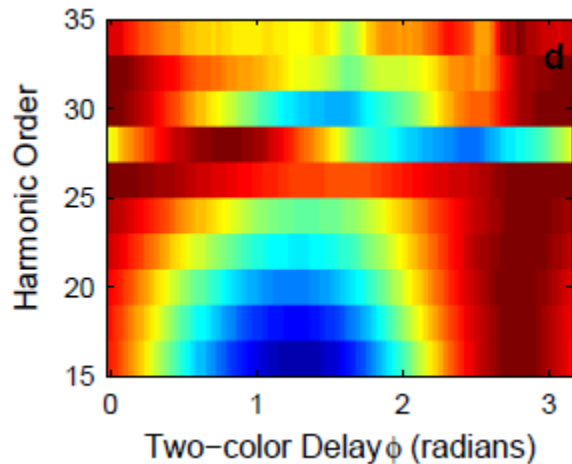
- Due to different ionization times, interference shifts optimal delay
- The shift is largest near destructive interference between the channels

Results

Normalized HHG signal
1.41014 W/cm² 800nm, 2% of orthogonally polarized 400nm

CO₂, aligned at 0 deg

He atom



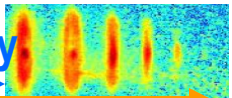
Theory

Experiment

$\pi/2$ phase shift marks the positions of dynamical minima.

Position of the phase jump identifies the initial phase between the hole states

D. Shafir et al, Nature 2012

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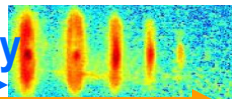
Conclusions

1. Tunneling delays:

- No delays in one-electron systems
- No delays in multielectron systems without coupling between different hole states
- Delays might be possible due to electron-hole interaction during tunneling

2. Electron-hole interaction during tunneling can lead to non-trivial tunneling dynamics

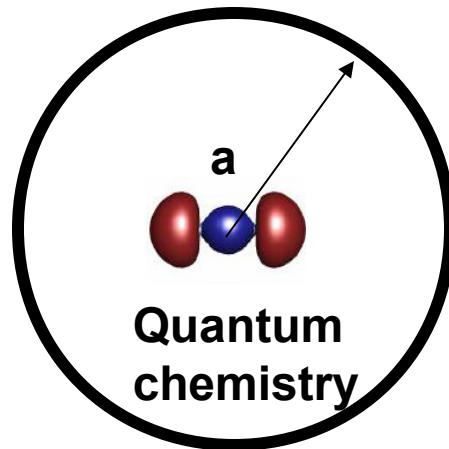
3. Using multidimensional high harmonic spectroscopy to resolve these dynamics is our next goal



Our Method

Analytical time-dependent R-Matrix (ARM):

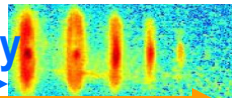
- R-matrix-type partitioning of configuration space
- The eikonal-Volkov approach in the outer region
- Quantum chemistry in the inner region (for molecules)
- Matching the two using the Bloch operator approach
- The saddle point method



WKB

(Eikonal-Volkov states
Smirnova et al PRA, 2008)

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Results: ARMed with ARM



One electron:

Analytical ionization amplitude for arbitrary potentials.

Benchmark:

- Same results as using the PPT method
 - for Hydrogen
 - for short range potentials
 - for linearly and circularly polarized fields

L. Torlina, O. Smirnova PRA, in press

J. Kaushal, O. Smirnova, in preparation

Advantages:

Arbitrary long-range potentials

Many electrons: Analytical ionization amplitudes including electron- electron correlation and core rearrangement during ionization

Gauge invariant, Technically much simpler than PPT

L. Torlina, M. Ivanov, Z. Walters, O. Smirnova, in press

